## Game of Set: Reasoning Supports Explanation

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## Summary

Game of Set: A popular card game of visual perception designed in 1974 by Marsha Falco, a geneticist, out of a coding scheme she developed in her research.
 of 12 (out of 81) where each $\quad \bigcirc \bigcirc \Delta 1 \Delta \Delta \Delta \bigcirc 8$ feature (color, shape, number and shading) is identical or all different.

Goal: Explore how to support reasoning and explanation
Contributions: Built an interactive online interface to play the game. Implemented and compared three algorithms to find all solutions
A. Enumeration
B. Backtrack search (two types)
C. Reformulation technique

## GUI and Constraint Model

The online interface allows a
user to play the game by clicking on cards to validate the selected cards as a set

The constraint model has three variables and five constraints


The challenge is not the computational but understand and replicate.

## Standard Solving Methods

## Enumeration:

- Three nested loops enumerate
all combinations of three cards
- Computationally easy $\Theta\left(n^{3}\right)$
- Cognitively, unsuitable



## Backtrack search:

- Two versions: with backchecking or with lookahead
- Enumerates all solutions in a tree-like manner
- Lookahead removes (future) options that are inconsistent with a given partial path. Thus, it generates fewer combinations
- Computationally easy $0\left(n^{3}\right)$
- Cognitively, unsuitable



## Motivating Example

Below we show how decomposing the set of 6 red cards on the feature 'number' helps uncovering all solutions.


## Reformulation

The idea is to focus on one feature (e.g., color) at a time, ignoring all others.

We decompose the problem for the various values of the chosen feature. The problems become smaller and easier to handle mentally. Then repeat for another feature, etc.

This decomposition strategy makes identifies where subproblems that are easier to solve or prove unsolvable and makes it easier to fund and explain solutions.


The choice of the feature is key to this strategy. We developed heuristics to assess the 'least diverse' feature which will reduce the number of subproblems generated.

## Future Work

1. Build a visualization of the reformulation strategy
2. Generate explanations of each operation step
3. Evaluate the usefulness of the strategy and explanations to human players

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